

DAV UNIVERSITY JALANDHAR



Course Scheme & Syllabus For Ph.D. Mathematics (Program ID-238)

Syllabi Applicable for Admissions in 2018 onwards

Scheme of Course

Sr. No.	Course Code	Course Name	Course Type	L	T	P	Credits
1	PHD 800	Research Methodology	Core	4	0	0	4
2	MTH 801	Seminar-I	Core	0	0	0	2
3	MTH xxx	Subject Specific	Departmental Elective	4	0	0	4
4	MTH xxx	Subject Specific	Departmental Elective	4	0	0	4

Total Credits: 14

L: Lectures

T: Tutorial

P: Practical

Cr: Credits

Departmental Elective (Choose any two courses)

Sr. No.	Course Code	Course Name	Course Type	L	T	P	Credits
1	MTH 802	Advanced Algebra	Departmental Elective	4	0	0	4
2	MTH 803	Commutative Algebra	Departmental Elective	4	0	0	4
3	MTH 804	Univalent Function Theory	Departmental Elective	4	0	0	4
4	MTH 805	Theory of Differential Subordination	Departmental Elective	4	0	0	4
5	MTH 806	Harmonic Mappings in the Plane	Departmental Elective	4	0	0	4
6	MTH 807	Continuum Mechanics	Departmental Elective	4	0	0	4
7	MTH 808	Computational Techniques	Departmental Elective	3	0	0	3
8	MTH 809	Computational Techniques Lab	Departmental Elective	0	0	2	1
9	MTH 810	ODE and System of ODE	Departmental Elective	4	0	0	4
10	MTH 811	Homological Algebra	Departmental Elective	4	0	0	4

Course Title: Research Methodology
Course Code: PHD 800

L	T	P	Credits
4	0	0	4

Objective: The major objective of this course is the understanding and application of emerging trends and new skills associated with research. The course will also introduce students to the safeguards against various errors in conducting any research.

UNIT-I **13 Hours**

Introduction to Research: Meaning of Research, Objectives of Research, Types of Research, Research Approaches, Research Process. Defining the Research Problem: What is a Research Problem? Selecting the Problem, Necessity of Defining the Problem, Review of Literature. Research Design: Meaning of Research Design, Need for Research Design, Features of a Good Design, and Important Concepts Relating to Research Design, Different Research Designs like various experimentation-Quasi, Latin Square, Factorial Design, their uses & methods.

UNIT-II **14 Hours**

Methods of Data Collection: Collection of Primary Data, Observation Method, Interview Method, Collection of Data through Questionnaires, Collection of Data through Schedules, Some Other Methods of Data Collection, Collection of Secondary Data, Selection of Appropriate Method for Data Collection. Measurement and Scaling: Non-comparative Scaling Techniques, Continuous Rating Scale, Itemized Rating Scale, Non-comparative Itemized Rating Scale Decisions, Multi-item Scales, Scale Evaluation, Choosing a Scaling Technique. Questionnaire & Form Design: Questionnaire & Observation Forms, Questionnaire Design Process.

UNIT-III **13 Hours**

Sampling design and Procedures: Sample or Census, The Sampling Design Process, A Classification of Sampling Techniques, Choosing Nonprobability Versus Probability Sampling, Uses of Nonprobability versus Probability Sampling. Data Preparation: Editing, Coding, Transcribing. Hypothesis Testing- T-test, Z-test, ANOVA-test, Chi-Square etc.

UNIT-IV **12 Hours**

Organization of Research Report: Types, Structure, Bibliography, References & Appendices. Style Manuals: APA style, MLA style, The Chicago Manual of style etc. Evaluation of Research Report, When and where to publish?, Ethical issues related to publishing, Plagiarism.

Reference Books:

1. Kumar, R. *Research Methodology: A step-by-step guide for Beginners*. London: SAGE, 2005.
2. Kothari, C. R. *Research methodology: Methods & Techniques (Rev. Ed.)* New Age International, New Delhi, 2006.
3. Malhotra, N. K. *Marketing research: An applied orientation, 6th ed.* SaddleRiver, N.J.: Pearson. Additional, 2010.

Course Title: Seminar-I
Course Code: MTH 801

L	T	P	Credits
0	0	0	2

Instructions and Guidelines for Seminar

1. Since PhD students must demonstrate the ability to interact with their peer group coherently, this course is designed to prepare students for research presentations.
2. This seminar will be related to the field of research.
3. During the course, researchers are expected to meet their guides regularly to seek guidance.
4. The final responsibility for giving effective presentations lies with researchers, not guides.
5. The evaluation will be based on contents and presentation skills of students.
6. Researchers must have a sound understanding of the research tools.
7. Students will have to meet the deadlines given by their respective guides and the department.
8. Each researcher will have to prepare a PPT on the topic approved by his/her guide.
9. Each researcher will be given 30-40 minutes for presentation
10. Slides must present researchers' work comprehensively.

Course Title: Advanced Algebra
Course Code: MTH 802

L	T	P	Credits
4	0	0	4

Objective: This is advanced course in Algebra for students who wish to pursue research work in Algebra. Galois Theory, canonical forms and structure of semisimple modules will be discussed in detail.

UNIT-I **13 Hours**

Introduction to Galois Theory: Automorphism groups and fixed fields, Fundamental theorem of Galois Theory, Proof of fundamental theorem of Algebra using Galois Theory.

UNIT-II **13 Hours**

Applications of Galois Theory to classical problems: Roots of unity and cyclotomic polynomials, cyclic extensions, Polynomials solvable by radicals, Symmetric functions, Ruler and compass constructions.

UNIT-III **12 Hours**

Modules over PID: The basic theory, Invariant factors, Elementary divisors, Fundamental theorem of finitely generated Abelian groups, The Rational canonical form, and The Jordan canonical form.

UNIT-IV **12 Hours**

Simple and semi simple modules and rings, Structure of semi simple rings: Wedderburn-Artin theorem.

Reference Books:

1. Bhattacharya, P.B., Jain S.K. and Nagpal, S.R. *Basic Abstract Algebra*, 2nd Edition. U.K.: Cambridge University Press, 2002.
2. Dummit, David S. and Foote, Richard M. *Abstract Algebra*, 2nd Edition, Wiley India, 2008.
3. Lam, T.Y., *A First Course in Non-commutative Rings*, 2nd Edition, Springer-Verlag New York, 2001.

Course Title: Commutative Algebra
Course Code: MTH 803

L	T	P	Credits
4	0	0	4

Objective: This course will give the student a solid grounding in commutative algebra which is used in both algebraic geometry and number theory.

UNIT-I

12 Hours

Rings and ideals - Rings and ring homomorphism, Ideals, quotient rings, zero-divisors, nilpotent elements, units, The prime spectrum of a ring, the nil radical and Jacobson radical, operation on ideals, extension and contraction.

UNIT-II

13 Hours

Modules - Modules and modules homomorphism, sub-modules and quotient modules, direct sums, free modules, finitely generated modules, Nakayama Lemma, simple modules, exact sequences of modules, Tensor product of modules.

UNIT-II

12 Hours

Rings and Modules of fractions, Local properties, extended and contracted ideals in ring of fractions, primary decomposition, 1st uniqueness theorem, 2nd uniqueness theorem.

UNIT-IV

13 Hours

Modules with chain conditions - Artinian and Noetherian modules, modules of finite length, Artinian rings, Noetherian rings, Hilbert basis theorem.

Reference Books:

1. Atiyah, M. F. and I.G. Macdonald. *Introduction to Commutative Algebra*. London: Addison-Wesley, 1969.
2. Musili, C. *Introduction to Rings and Modules*. New Delhi: Narosa Publishing House, 1994.
3. Reid, Miles. *Under-graduate Commutative Algebra*, Cambridge, UK: Cambridge University Press, 1996.
4. Gopalakrishnan, N. S. *Commutative Algebra*. New Delhi: Oxonian Press, 1984.
5. Dummit, David S., and Richard M. Foote. *Abstract Algebra*. Hoboken, NJ: John Wiley & Sons, Inc., 2004.
6. Matsumura, H. *Commutative Ring Theory*. Cambridge, UK: Cambridge University Press, 1989.

Course Title: Univalent Function Theory
Course Code: MTH 804

L	T	P	Credits
4	0	0	4

Objective: The objective of this course is to teach advanced concepts and topics in theory of Univalent Functions.

UNIT-I **13 Hours**

Normal families, Extremal problems, The Riemann Mapping Theorem, Analytic continuation, Harmonic and Sub-harmonic functions, Green's functions, Positive Harmonic functions.

UNIT-II **14 Hours**

Univalent Functions: Elementary Properties and results, Examples of univalent functions, The Area theorem, Growth and Distortion theorems, Coefficient estimates for univalent functions. The maximum modulus of univalent functions.

UNIT-III **14 Hours**

Subclasses of Univalent Functions: Classes of Convex, Starlike and Close-to-convex functions and their properties in the unit disk, Spirallike functions, Typically Real functions, Growth of Integral Means, Odd Univalent functions, Asymptotic Bieberbach Conjecture.

UNIT-IV **14 Hours**

Bounded functions, radius of Univalence, Convexity and Starlikeness, Combinations, Convolution and Subordination of Univalent functions.

Reference Books:

1. Duren, P. *Univalent Functions*. New York: Springer, 1983.
2. Goodman, A. W. *Univalent Functions-Volume I & II*. Mariner, Florida, 1983.
3. Pommerenke, C. *Univalent Functions*. Van den Hoek and Ruprecht, Göttingen, 1975.
4. Graham, I. and Kohr, G. *Geometric Function Theory in One and Higher Dimensions*. New York: Marcel Dekker, 2003.

Course Title: Theory of Differential Subordination
Course Code: MTH 805

L	T	P	Credits
4	0	0	4

Objective: This course will give the student a solid grounding in differential subordination and differential superordination for future research.

UNIT-I

14 Hours

Subordination, Hypergeometric functions, Convex and Starlike functions, Close-to-convex functions, Spirallike functions, Integral Operators: Alexander operator, Libera operator, Bernardi operator. The general theory of differential subordinations, Admissible functions and fundamental results.

UNIT-II

13 Hours

Jack-Miller-Mocanu Lemma, Admissible functions and fundamental theorems, open door lemma and integral existence theorem, Classical Results of Geometric Function Theory Revisited.

UNIT-III

14 Hours

First order linear differential subordination, Briot-Bouquet differential subordinations, Briot-Bouquet applications in Univalent function theory, Generalized Briot-Bouquet differential subordinations, Analytic Integral operators between classes of functions, Subordination-preserving Integral operators.

UNIT-IV

14 Hours

Second order linear differential subordinations, Integral operators preserving functions with positive real part, Integral operators preserving bounded functions, Averaging Integral operators, Hypergeometric functions, Schwarzian derivative, Applications to starlikeness and convexity.

Reference Books:

1. Miller, S. S. and Mocanu, P. T. *Differential Subordinations: Theory and Applications*. New York: Marcel Dekker Inc., 2000.
2. Bulboaca, T. *Differential Subordinations and Superordination: Recent Results*. Cluj Napoca, 2005.

Course Title: Harmonic Mappings in the Plane
Course Code: MTH 806

L	T	P	Credits
4	0	0	4

Objective: This course is design to understand basics and applications of the emerging research topic Planar Harmonic Mappings.

UNIT-I

13 Hours

Complex valued harmonic mappings and their properties, decomposition of harmonic mappings into analytic and co-analytic parts, Jacobian and dilatation of harmonic mappings. The Argument principle, The Dirichlet problem, Lewy's Theorem.

UNIT-II

12 Hours

Construction of harmonic mappings (shear construction). Boundary behavior of harmonic mappings. Subclasses of Univalent Harmonic Mappings: Class S_H and its properties, Subclasses of S_H : Coefficients bounds of Convex, Starlike and Close-to-convex univalent harmonic mappings.

UNIT-III

12 Hours

Linear combination and convolutions: Univalence of linear combination and convolution of harmonic mappings. Convolutions of harmonic right half plane mapping and related results.

UNIT-IV

13 Hours

Basics of differential geometry and minimal surfaces, Isotheremal parameters, Weierstrass representation of minimal surfaces, connection of planar harmonic mappings and minimal surfaces.

Reference Books:

1. Brilleslyper, M. A. and Michael J. Dorff et. al. *Explorations in complex analysis*, Mathematical Association of America. 2015.
2. Duren, P. *Harmonic mappings in the plane*, Cambridge university press. U.K. 2004.
3. Graham, I. and Kohr, G. *Geometric Function Theory in One and Higher Dimensions*. New York: Marcel Dekker, 2003.

Course Title: Continuum Mechanics
Course Code: MTH 807

L	T	P	Credits
4	0	0	4

Objective: The objective of this course is to introduce the concept of strains tensors, stress tensors and basic concepts of elastic body deformation and to make students familiar about the constitutive relations and field equations. Dynamics of elastic bodies and basic problems related to elastic wave propagation are also introduced.

UNIT-I **12 Hours**

Tensors: Summation convention, coordinate transformation, tensors of several orders, algebra of tensors, symmetric and skew-symmetric tensors, Kronecker's delta, Gradient, Divergence, Curl tensor notations, contra-variant and covariant tensors.

UNIT-II **11 Hours**

Stress and Strain: Deformation in elastic bodies, affine transformation, strain-displacement relation, principal direction, stress and strain tensors, components of stress and strain, generalised Hooke's Law- relation between stress and strain, elastic constants and their physical significance.

UNIT-III **13 Hours**

Dilatation and Distortion waves: Two dimensional propagation of elastic waves in isotropic solid, waves of dilatation and waves of distortion, equation of motion in classical theory of elasticity, Helmholtz decomposition theorem.

UNIT-IV **12 Hours**

Surface Waves: Introduction to surface waves, Rayleigh and Love waves, Frequency equations of Rayleigh waves and Love waves, Radial vibrations of elastic sphere, Reflection and transmission of P/SV and SH waves from liquid/solid, solid/solid interface.

Reference Books:

1. Narayan, S. *A text book of Cartesian Tensors (with an introduction to general tensors)*, 3rd Edition. New Delhi: S. Chand publications, 1968.
2. Young, E.C. *Vectors and tensor analysis*, 2nd Edition. USA: CRC Press, 1993.
3. Sokolnikoff, I.S. *Mathematical theory of elasticity*, 2nd Edition. New York: McGraw-Hill, 1982.
4. Kolsky, H. *Stress waves in Solids*, 2nd Edition. USA: Dover Publications, Reprint 2002.
5. Ghosh, P.K. *Mathematics of waves and vibrations*. New Delhi: The Macmillan Company of India Ltd., 1975.
6. Ewing, W.M., W.S. Jardetzky, and F. Press. *Elastic waves in layered media*, New-York: McGraw-Hill Book Co., 1957.

Course Title: Computational Techniques
Paper Code: MTH 808

L	T	P	Credits
3	0	0	3

Objective: The objective of this course is to introduce the software MATLAB for high-performance numerical computation and visualization. For the purpose of learning programming skill, some Numerical methods which are extremely useful in scientific research are included. For practicing the programs of the numerical methods, the course of practical has also been included in this paper.

UNIT-I

13 Hours

Errors, Error propagation, Order of approximation.

Solution of non-linear equations: Review of Bisection, Regula-Falsi and Secant method. Newton-Raphson method and its family, Functional iteration method. Rate of convergence of these methods. Newton's method for complex roots and multiple roots, Simultaneous non-linear equations by Newton-Raphson method.

UNIT-II

12 Hours

Operators: Forward, Backward and Shift (Definitions and some relations among them).

Interpolation: Divided differences, Newton's formulae for interpolation, Lagrange and Hermite interpolation, Cubic Spline interpolation.

Solution of Ordinary Differential Equations: Picard method of Successive approximations, Taylor series method, Euler's method, Modified Euler's method, Runge - Kutta methods, Predictor-Corrector methods.

UNIT-III

13 Hours

Starting and quitting MATLAB, basic operations of MATLAB, input/output data, the colon operator, types of files, creating and executing a script file, mathematical functions, random number generators. Constants, expressions, variables, numbers, operators, functions, working with arrays and matrices, matrix manipulations, creating vectors, arithmetic operations, relational operations, logical operations, Eigen values and Eigen vectors.

UNIT-IV

12 Hours

Looping statements: if, else, and else-if, for, while, switch and case, break, return, developing algorithms using nested loops.

Graphics, basic 2D plots, style options, labels, title, legend and other text objects, axis control, zoom in, zoom out, 3D plots, view, rotate view, mesh and surface plots.

Reference Books:

1. Conte, S.D., and Carl De Boor, *Elementary Numerical Analysis, An Algorithmic Approach*. New Delhi: Tata McGraw Hill, 1981.
2. Bradie, B., *A Friendly Introduction to Numerical Analysis*. India: Pearson Education, 2007.
3. Gerald C.F., and P.O. Wheatley, *Applied Numerical Analysis*. India: Pearson Education, 2008.
4. Pratap, R. *Getting Started with MATLAB*, Oxford University Press, New Delhi, 2015.
5. Chapman, S.J., *MATLAB Programming for Engineers, 4th Edition*, Cengage Learning, Boston, USA. 2015.

Course Title: Computational Techniques Lab
Paper Code: MTH 809

L	T	P	Credits
0	0	2	1

Objective: Writing Programs in MATLAB for the problems based on the methods studied in theory paper and to run the Program on PC.

List of Practicals

1. Matrix multiplication
2. Secant method and error analysis
3. Newton-Raphson method and error analysis
4. Newton-Raphson's method for system of non-linear equations and error analysis
5. Newton's forward/backward interpolation
6. Lagrange interpolation
7. Hermite interpolation
8. Modified Euler's method
9. Runge-Kutta method of order four
10. Predictor-Corrector methods

Reference Books:

1. Pratap, R. *Getting Started with MATLAB*, Oxford University Press, New Delhi, 2015.
2. Chapman, S.J., *MATLAB Programming for Engineers, 4th Edition*, Cengage Learning, Boston, USA. 2015.
3. Duffy, D.G. *Advanced engineering mathematics with MATLAB*, CRC Press (Chapman and Hall), Boca Raton, Florida, 2003.
4. Kalechman, M. *Practical MATLAB basics for engineers*, CRC Press (Chapman and Hall), Boca Raton, Florida, 2009.
5. Mathews, John H., and D. Fink Kurtis. *Numerical Methods using Matlab 4th Edition*. New Delhi: PHI Learning Private Limited, 2012.

Course Title: ODE and System of ODE

Paper Code: MTH 810

L	T	P	Credits
4	0	0	4

Objective: The objective of this course is to equip the students with fundamental knowledge and problem solving skills in Power series methods of solution of ODE, Existence and Uniqueness theory of Initial Value Problems and Solution of system of differential equations.

UNIT-I

14 Hours

Review of fundamentals of Ordinary differential equations. The method of successive approximation. Initial value problem, Ascoli's Lemma, Gronwall's inequality, Cauchy Peano Existence Theorem, Picard's existence and uniqueness theorem, Lipschitz condition.

UNIT-II

16 Hours

Linear system of equations (homogeneous & non-homogeneous). Superposition principle, Fundamental set of solutions, Fundamental Matrix, Wronskian, Abel Liouville formula, Reduction of order, Adjoint systems and Self Adjoint systems of second order. Linear 2nd order equations, preliminaries, Sturm's separation theorem, Sturm's fundamental comparison theorem.

UNIT-III

15 Hours

Orthogonal set of functions, Orthonormal set of functions, Gram-Schmidt process of orthonormalization, Sturm Liouville's boundary value problems, Orthogonality of Eigenfunctions and reality of Eigenvalues. Adjoint forms, Lagrange identity, Green function to solve boundary value problems.

UNIT-IV

15 Hours

Power series solution of differential equation about an ordinary point, Solution about regular singular points: The method of Frobenius, Applications, Legendre's, Hermite's and Bessel's equation. Ordinary differential equations in more than two variables: Simultaneous Differential equations of the first order and the first degree in three variables, Methods of their solution and applications.

Reference Books:

1. Coddington, E. A. *An Introduction to Ordinary Differential Equations*. Prentice-Hall of India Private Ltd., New Delhi, 2001.
2. Piaggio, H. T. H. *Differential Equations*. New Delhi: CBS Publisher, 2004.
3. George, F Simmons. *Differential equations with applications and historical notes*. New Delhi: Tata McGraw Hill, 1974.
4. Sneddon, I. N. *Elements of Partial Differential Equations*. New Delhi: Tata McGraw Hill 1957.
5. Ross, S. L. *Differential Equations*. New Delhi: John Wiley and Sons 2004.

Course Title: Homological Algebra
Course Code: MTH 811

L	T	P	Credits
4	0	0	4

Objective: The objective of this course is to introduce the basic concepts of modern Category Theory and Homological Algebra.

UNIT-I

12 Hours

Homology functors : Diagrams over a ring, Translations of diagrams, Translation category, split exact sequence, images and kernel as functors, Homology functors, The connecting homomorphism, Complexes, boundary homomorphism, differentiation homomorphism, homology modules, right and left complexes, exact homology sequence and Homotopic translations.

UNIT-II

12 Hours

Projective and injective modules : Projective modules, injective modules, An existence theorem for injective modules, Complexes over a modules, right and left complexes over a module, augmentation translation and augmentation homomorphism, acyclic right and acyclic left complexes over a module, Projective and injective resolutions of a module, Properties of resolutions of a module.

UNIT-III

13 Hours

Derived Functors: Projective and injective resolutions of an exact sequence, Properties of resolutions of sequences, Functors of complexes, Associated translations, Functors of two complexes, Right-derived functors, the defining systems and the connecting homomorphisms, the functor R^0T , Left-derived functors, the functor L_0T .

UNIT-IV

13 Hours

Torsion and Extension Functors: Connected sequences of functors, connected right and left sequences of covariant and contravariant functors, homomorphism and isomorphism as a natural equivalence between connected sequences of functors. Torsion functors $Torn$, Basic properties of Torsion functors, Extension functors and Basic properties of extension functors.

Reference Books:

1. Northcott, D. G. *An introduction to Homological Algebra*. Cambridge University Press, UK, 2009.
2. Rotman, J. *An introduction to Homological Algebra*. Springer, New York, 2009.